

Name: HW 1.4 (b) Key

1. Bryce is scheduled to receive two future payments of 1700. The first payment will occur at the end of year n , and the second payment occurs 11 years after the first payment. Assuming an annual effective interest rate of 6.7%, the present value of the two payments is 957.56. Find n .

☒ A) 15 B) 12 C) 13 D) 14 E) 16

$$i = 6.7\%$$

$$957.56 = 1700v^n + 1700v^{n+11}$$

$$957.56 = v^n(1700 + 1700v^{11})$$

$$v^n = 0.3780$$

$$n = \frac{\ln(0.3780)}{\ln(v)} = \boxed{15}$$

2. You are given two loans, with each loan to be repaid by a single payment in the future. Each payment includes both principal and interest.

The first loan is repaid by a 2200 payment at the end of 3 years. The interest is accrued at 9% per annum compounded semiannually.

The second loan is repaid by a 1600 payment at the end of 8 years. The interest is accrued at 11% per annum compounded semiannually.

The two loans are to be consolidated. The consolidated loan is to be repaid by two equal installments of X , with interest at 14% per annum compounded semiannually. The first payment is due immediately and the second payment is due one year from now.

Calculate X . [2.a-b #06]

☒ A) 1264 B) 1226 C) 1239 D) 1252 E) 1277

$$PV = 2200(1.045)^{-6} + 1600(1.055)^{-16} = 2368.70$$

$$2368.70 = X + X(1.07)^{-2}$$

$$X = \boxed{1264.36}$$

3. You are given the following data on three series of payments.

	Payment at end of year			AV at end of year 21
	7	14	21	
Series A	320	180	270	X
Series B	0	430	790	X + 180
Series C	Y	620	0	X

Assume interest is compounded annually.

Calculate Y. [2.a-b #09]

- ☒ A) 146 B) 151 C) 155 D) 160 E) 164

$$A: 320(1+i)^{14} + 180(1+i)^7 + 270 = X$$

$$B: 430(1+i)^7 + 790 = X + 180$$

$$A - B: 320(1+i)^{14} - 250(1+i)^7 - 520 = -180$$

$$320(1+i)^{14} - 250(1+i)^7 - 340 = 0 \rightarrow i = 5.8920\%, X = 1251.96$$

$$Y(1+i)^{14} + 620(1+i)^7 = X \rightarrow Y = \boxed{146.42}$$

4. Payments of 100, 200, and 400 are made at the ends of years 5, 9, and 12, respectively. Assuming an annual effective interest rate of 8%, this sequence of payments is equivalent to a single payment of 700 at time T . Let S be the approximation of T obtained using the method of equated time. Find $S - T$.

- ☒ A) 0.25 B) 0.20 C) 0.23 D) 0.28 E) 0.30

$$i = 8\%$$

$$700v^T = 100v^5 + 200v^9 + 400v^{12} \rightarrow v^T = 0.4671 \rightarrow T = 9.89$$

$$S = \frac{100(5) + 200(9) + 400(12)}{100 + 200 + 400} = 10.14$$

$$S - T = \boxed{0.25}$$

5. Vicky borrows P at an annual effective rate of 5%. She agrees to repay the loan by making the following payments: A payment of 450 at the end of year 2, a payment of 400 at the end of year 4, a payment of 200 at the end of year 6, and a payment of X at the end of year 7.

The method of equated time can be used to determine that Vicky could have also repaid the loan by making a payment of $1050 + X$ at approximately time $t = 4.7188$. Find X .

- ☒ A) 550 B) 350 C) 400 D) 450 E) 500

$$4.7188 = \frac{450(2) + 400(4) + 200(6) + X(7)}{450 + 400 + 200 + X} = \frac{3700 + 7X}{1050 + X}$$

$$4954.74 + 4.7188X = 3700 + 7X$$

$$X = \boxed{550}$$