

## HW 2.1 Key

1. Townsville High School has official teams for two sports: baseball and soccer. You are given the following information regarding student participation in these sports:

- 48% of students play baseball.
- 38% of students play soccer.
- 40% of students play neither sport.

Determine the percentage of students that play exactly one sport.

- A) 34%  
 B) 29%  
 C) 30%  
 D) 31%  
 E) 33%

$$P(B) = 0.48 \quad P(S) = 0.38 \quad P[(BUS)^c] = 0.4$$

$$P(B \cup S) = 0.6 = 0.48 + 0.38 - P(B \cap S)$$

$$P(B \cap S) = 0.26$$

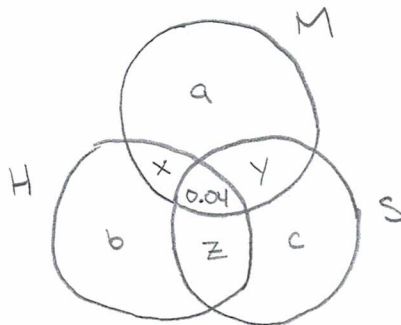
$$P(\text{ex. one}) = P(B \cup S) - P(B \cap S) = \boxed{0.34}$$

2. Townsville High School has three academic clubs: History, Math, and Science. You are given the following information regarding student participation in these clubs:

- 27% of students participate in History Club.
- 32% of students participate in Math Club.
- 28% of students participate in Science Club.
- 4% of students participate in all three clubs.
- 39% of students participate in no clubs.

Determine the percentage of students that participate in more than one club.

- A) 22%  
 B) 19%  
 C) 21%  
 D) 23%  
 E) 25%



$$P(H) = 0.27$$

$$P(M) = 0.32$$

$$P(S) = 0.28$$

$$P(H \cap M \cap S) = 0.04$$

$$P[\neg(H \cup M \cup S)] = 0.39$$

$$P[H \cup M \cup S] = 0.61$$

$$\text{We want: } x + y + z + 0.04$$

$$\textcircled{1} (a+b+c) + (x+y+z) + 0.04 = 0.61$$

$$\textcircled{2} P(H) + P(M) + P(S) = (a+b+c) + 2(x+y+z) + 3(0.04) = 0.27 + 0.32 + 0.28$$

$$\left. \begin{array}{l} \textcircled{1} \Rightarrow (a+b+c) + (x+y+z) = 0.57 \\ \textcircled{2} \Rightarrow (a+b+c) + 2(x+y+z) = 0.75 \end{array} \right\} \Rightarrow x+y+z = 0.18$$

$$\text{Answer} = \boxed{0.22}$$

3. Assume that events  $A$  and  $B$  satisfy the following properties:

- The probability of event  $A$  occurring is 1.4 times the probability of event  $B$  occurring.
- The probability of at least one of the events occurring is 0.41.
- The probability of both events occurring is 0.07.

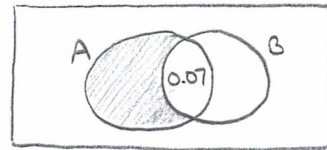
Determine the probability of Event  $A$  occurring and Event  $B$  not occurring.

- A) 0.210
- B) 0.172
- C) 0.185
- D) 0.197
- E) 0.223

$$P(A) = 1.4 P(B)$$

$$P(A \cup B) = 0.41$$

$$P(A \cap B) = 0.07$$



$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

$$0.41 = 1.4 P(B) + P(B) - 0.07$$

$$0.48 = 2.4 P(B)$$

$$P(B) = 0.2$$

$$P(A) = 0.28$$

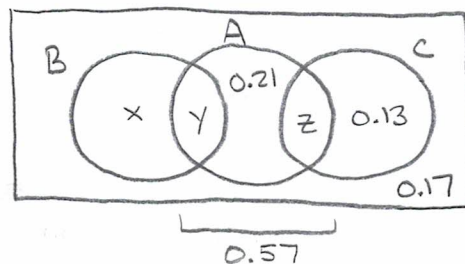
$$P(A \cap B^c) = 0.28 - 0.07 = \boxed{0.21}$$

4. You are given the following information about events  $A$ ,  $B$ , and  $C$ .

- The probability of event  $A$  occurring is 0.57.
- The probability of only event  $A$  occurring is 0.21.
- Events  $B$  and  $C$  are mutually exclusive.
- The probability of  $C$  occurring is 1.5 times the probability of  $B$  occurring.
- The probability of none of the events occurring is 0.17.
- The probability  $C$  occurring and  $A$  not occurring 0.13.

Find the probability of event  $B$  NOT occurring.

- A) 0.752
- B) 0.684
- C) 0.707
- D) 0.729
- E) 0.775



$$\textcircled{1} \quad y + z = 0.57 - 0.21 = 0.36$$

$$\textcircled{2} \quad z + 0.13 = 1.5(x + y)$$

$$\textcircled{3} \quad x + y + z = 0.83 - 0.21 - 0.13 = 0.49$$

$$\textcircled{2} \text{ minus } \textcircled{1} \Rightarrow x = 0.49 - 0.36 = 0.13$$

$$\textcircled{2} \Rightarrow z + 0.13 = 1.5(0.13 + y) \Rightarrow 1.5y - z = -0.065$$

$$1.5y - z = -0.065 \quad ] \Rightarrow 2.5y = 0.295$$

$$y + z = 0.36$$

$$y = 0.118$$

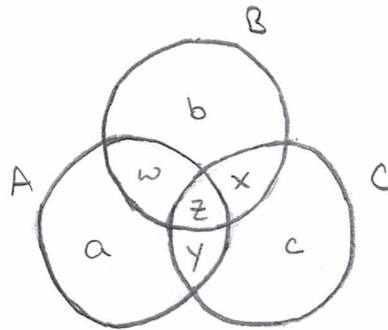
$$P(B) = x + y = 0.248$$

$$P(B^c) = \boxed{0.752}$$

5. You are given the following information about events  $A$ ,  $B$ , and  $C$ .
- 1 • The probability of  $A$  occurring is 0.35.
  - 2 • The probability of  $B$  occurring is 0.37.
  - 3 • The probability of  $C$  occurring is 0.3.
  - 4 • The probability of at least two of the events occurring is 0.29.
  - 5 • The probability of  $B$  and  $C$  occurring is 0.16.
  - 6 • The probability of  $A$  and  $B$  occurring is 0.03 greater than the probability of  $A$  and  $C$  occurring.
  - 7 • The probability of only  $A$  occurring is 0.03 greater than the probability of only  $C$  occurring.

Find the probability of exactly one of the three events occurring.

- A) 0.34  
 B) 0.33  
 C) 0.35  
 D) 0.36  
 E) 0.37



$$\begin{aligned}
 \textcircled{4} \quad w + x + y + z &= 0.29 \\
 \textcircled{5} \quad x + z &= 0.16 \\
 \textcircled{6} \quad w + z &= y + z + 0.03 \rightarrow w - y = 0.03 \\
 \textcircled{7} \quad 0.35 - w - z - y &= (0.3 - x - z - y) + 0.03 \\
 0.35 - 0.08 &= 0.33 - x \\
 x &= 0.06 \\
 \textcircled{4} \quad 0.08 + 0.06 + 0.05 + z &= 0.29 \rightarrow z = 0.10 \\
 \textcircled{1} \quad a + 0.08 + 0.10 + 0.05 &= 0.35 \rightarrow a = 0.12 \\
 \textcircled{2} \quad b + 0.08 + 0.10 + 0.06 &= 0.37 \rightarrow b = 0.13 \\
 \textcircled{3} \quad c + 0.05 + 0.10 + 0.06 &= 0.3 \rightarrow c = 0.09
 \end{aligned}$$

$$a + b + c = \boxed{0.34}$$