

Section 01.a	Section 01.a	Section 01.a
Simple Interest Formula	Write i_t and d_t in terms of the accumulation function, $a(t)$	Compound Interest 1) Give $a(t)$ in terms of i 2) Give $a(t)$ in terms of d 3) Give $a(t)$ in terms of δ
Section 01.a	Section 01.a	Section 01.a
Identities 1) Give i in terms of d 2) Give d in terms of i	Identities 1) Give v in terms of i 2) Give v in terms of d	Nominal Rates 1) Give $a(t)$ in terms of $i^{(m)}$ 2) Give $a(t)$ in terms of $d^{(m)}$
Section 01.b – d	Section 01.e	Section 01.g
Force of Interest: 1) Define FoI in terms of $a(t)$ 2) Give $a(t)$ in terms of δ_t	Constant Force of Interest 1) Give δ in terms of i 2) Give $a(t)$ in terms of δ	Variable FoI Trap Given $a(t)$, find AV of 1 invested at time t_1 and accumulated to t_2
Section 01.g	Section 02.b	Section 03.a
Variable FoI Trap Given $a(t)$, find PV at time t_1 of a payment of 1 at time t_2	Method of Equated Time	Geometric Series Sum the following: $a + ar + ar^2 + \dots + ar^{n-1}$
Section 03.b	Section 03.b	Section 03.b
Annuity Immediate 1) Give formula for $a_{\overline{n} i}$ 2) Give formula for $s_{\overline{n} i}$	Annuity Due 1) Give formula for $\ddot{a}_{\overline{n} i}$ 2) Give formula for $\ddot{s}_{\overline{n} i}$	Annuity Identities 1) Give $\ddot{a}_{\overline{n} i}$ in terms of $a_{\overline{n} i}$ 2) Give $\ddot{s}_{\overline{n} i}$ in terms of $s_{\overline{n} i}$

$a(t) = (1 + i)^t$ $a(t) = (1 - d)^{-t}$ $a(t) = e^{\delta t}$	$i_t = \frac{a(t) - a(t-1)}{a(t-1)}$ $d_t = \frac{a(t) - a(t-1)}{a(t)}$	$a(t) = 1 + it$
$a(t) = (1 + i)^t = \left(1 + \frac{i^{(m)}}{m}\right)^{mt}$ $a(t) = (1 - d)^{-t} = \left(1 - \frac{d^{(m)}}{m}\right)^{-mt}$	$v = \frac{1}{1+i}$ $v = 1-d$	$i = \frac{d}{1-d}$ $d = \frac{i}{1+i}$
$a(t_1 \text{ to } t_2) = e^{\int_{t_1}^{t_2} \delta, dr} = \frac{a(t_2)}{a(t_1)}$	$\delta = \ln(1 + i)$ $a(t) = e^{\delta t}$	$\delta_t = \frac{a'(t)}{a(t)}$ $a(t) = e^{\int_0^t \delta, dr}$
$\frac{a(1 - r^n)}{1 - r}$ $= \frac{\text{First Term} - \text{First Omitted Term}}{1 - \text{Common Ratio}}$	$\bar{t} = \frac{P_1 t_1 + P_2 t_2 + \dots + P_n t_n}{P_1 + P_2 + \dots + P_n}$	$\frac{1}{a(t_1 \text{ to } t_2)} = e^{-\int_{t_1}^{t_2} \delta, dr} = \frac{a(t_1)}{a(t_2)}$
$\ddot{a}_{\overline{n} i} = (1 + i)a_{\overline{n} i}$ $\ddot{s}_{\overline{n} i} = (1 + i)s_{\overline{n} i}$	$\ddot{a}_{\overline{n} i} = \frac{1 - v^n}{d}$ $\ddot{s}_{\overline{n} i} = \frac{(1 + i)^n - 1}{d}$	$a_{\overline{n} i} = \frac{1 - v^n}{i}$ $s_{\overline{n} i} = \frac{(1 + i)^n - 1}{i}$

Section 03.b	Section 03.b	Section 03.b
<p>Annuity Relationships</p> <p>State the +1/-1 formulas.</p>	<p>Definition of Annuity Formulas</p> <p>1) Write $s_{\overline{n} i}$ in terms of $(1+i)$.</p> <p>2) Write $\ddot{s}_{\overline{n} i}$ in terms of $(1+i)$.</p>	<p>Definition of Annuity Formulas</p> <p>1) Write $a_{\overline{n} i}$ in terms of v.</p> <p>2) Write $\ddot{a}_{\overline{n} i}$ in terms of v.</p>
Section 03.d	Section 03.f	Section 03.f
<p>Deferred Annuities</p> <p>1) Give ${}_m a_{\overline{n} i}$ in terms of $a_{\overline{n} i}$</p> <p>2) Give ${}_m a_{\overline{n} i}$ using block pmts.</p>	<p>Infinite Geometric Series</p> <p>Sum the following: $a + ar + ar^2 + ar^3 + \dots$</p>	<p>Perpetuities</p> <p>1) Give the formula for $a_{\overline{\infty} i}$</p> <p>2) Give two formulas for $\ddot{a}_{\overline{\infty} i}$</p>
Section 03.g	Section 04.b	Section 04.b
<p>The $a_{\overline{2n} } / a_{\overline{n} }$ Trick</p> <p>1) Simplify $a_{\overline{2n} } / a_{\overline{n} }$</p> <p>2) Simplify $a_{\overline{3n} } / a_{\overline{n} }$</p>	<p>Fission</p> <p>PV and AV of payments of P occurring at the end of every n years for kn years.</p>	<p>Fusion</p> <p>PV and AV of payments of P occurring at the end of each m-thly period, for n years.</p>
Section 04.b	Section 04.b	Section 04.b
<p>m-thly Annuities</p> <p>PV and AV of an n-year annuity paying $1/m$ at the end of each m-thly period.</p>	<p>m-thly Annuities</p> <p>PV and AV of an n-year annuity paying $1/m$ at the beginning of each m-thly period.</p>	<p>m-thly Perpetuities</p> <p>PV of a perpetuity paying $1/m$ at the end of each m-thly period.</p>
Section 04.d	Section 04.e	Section 04.g
<p>Continuous Annuities</p> <p>PV and AV of continuous payments of 1 per year for n years.</p>	<p>Double Dots Cancel</p> <p>State the "Double Dots Cancel" rule.</p>	<p>Annuities with varying interest</p> <p>Write $a_{\overline{n} }$ and $s_{\overline{n} }$ in terms of $a(t)$.</p>

$a_{\overline{n} i} = v + v^2 + \dots + v^n$ $\ddot{a}_{\overline{n} i} = 1 + v + v^2 + \dots + v^n$	$s_{\overline{n} i} = 1 + (1+i) + \dots + (1+i)^n$ $\ddot{s}_{\overline{n} i} = (1+i) + (1+i)^2 + \dots + (1+i)^n$	$\ddot{s}_{\overline{n} i} = s_{\overline{n+1} i} - 1$ $\ddot{a}_{\overline{n} i} = a_{\overline{n-1} i} + 1$
$a_{\overline{\infty} i} = \frac{1}{i}$ $\ddot{a}_{\overline{\infty} i} = \frac{1}{d} = a_{\overline{\infty} i} + 1$	$\frac{a}{1-r}$	${}_m a_{\overline{n} i} = v^m a_{\overline{n} i}$ ${}_m a_{\overline{n} i} = a_{\overline{m+n} i} - a_{\overline{n} i}$
$PV = (P s_{\overline{m} j}) a_{\overline{n} i}$ $AV = (P s_{\overline{m} j}) s_{\overline{n} i}$	$PV = \left(\frac{P}{s_{\overline{n} i}} \right) a_{\overline{kn} j}$ $AV = \left(\frac{P}{s_{\overline{n} i}} \right) s_{\overline{kn} j}$	$\frac{a_{\overline{2n} }}{a_{\overline{n} }} = 1 + v^n$ $\frac{a_{\overline{3n} }}{a_{\overline{n} }} = 1 + v^n + v^{2n}$
$a_{\overline{\infty} }^{(m)} = \frac{1}{i^{(m)}}$ $\ddot{a}_{\overline{\infty} }^{(m)} = \frac{1}{d^{(m)}} = a_{\overline{\infty} }^{(m)} + \frac{1}{m}$	$\ddot{a}_{\overline{n} }^{(m)} = \frac{1 - v^n}{d^{(m)}}$ $\ddot{s}_{\overline{n} }^{(m)} = \frac{(1+i)^n - 1}{d^{(m)}}$	$a_{\overline{n} }^{(m)} = \frac{1 - v^n}{i^{(m)}}$ $s_{\overline{n} }^{(m)} = \frac{(1+i)^n - 1}{i^{(m)}}$
$a_{\overline{n} } = \left(\frac{1}{a(1)} + \frac{1}{a(2)} + \dots + \frac{1}{a(n)} \right)$ $s_{\overline{n} } = a(n) \left(\frac{1}{a(1)} + \frac{1}{a(2)} + \dots + \frac{1}{a(n)} \right)$	$\frac{a_{\overline{n} }}{a_{\overline{p} }} = \frac{\ddot{a}_{\overline{n} }}{\ddot{a}_{\overline{p} }} = \frac{a_{\overline{n} }^{(m)}}{a_{\overline{p} }^{(m)}} = \frac{\ddot{a}_{\overline{n} }^{(m)}}{\ddot{a}_{\overline{p} }^{(m)}}$	$\bar{a}_{\overline{n} } = \int_0^n v^t dt = \frac{1 - v^n}{\delta}$ $\bar{s}_{\overline{n} } = (1+i)^n \bar{a}_{\overline{n} } = \frac{(1+i)^n - 1}{\delta}$

Section 04.h	Section 04.h	Section 04.h																				
<p>Arithmetic Progression</p> <p>P/Q formulas for AV and PV of an arithmetic annuity.</p>	<p>Increasing Annuities</p> <p>1) Give the formula for $(Ia)_{\overline{n} }$.</p> <p>2) Give the formula for $(Is)_{\overline{n} }$.</p>	<p>Decreasing Annuities</p> <p>1) Give the formula for $(Da)_{\overline{n} }$.</p> <p>2) Give the formula for $(Ds)_{\overline{n} }$.</p>																				
Section 04.h	Section 04.h	Section 04.i																				
<p>Increasing Perpetuities</p> <p>Give the formula for $(Ia)_{\overline{\infty} }$</p>	<p>Increasing to Level Perpetuities</p> <p>PV of a perpetuity imm. paying: 1, 2, ..., n, n, n, n, ...</p>	<p><i>m</i>-thly Increasing Annuities</p> <p>1) Describe payments for $(Ia)_{\overline{n} }^{(m)}$</p> <p>2) Give formula for $(Ia)_{\overline{n} }^{(m)}$</p>																				
Section 04.i	Section 04.j	Section 04.k																				
<p><i>m</i>-thly Increasing Annuities</p> <p>1) Describe payments for $(I^{(m)}a)_{\overline{n} }^{(m)}$</p> <p>2) Give formula for $(I^{(m)}a)_{\overline{n} }^{(m)}$</p>	<p>Geometric Annuities</p> <p>PV of an <i>n</i>-year annuity immediate with payments starting at <i>P</i> and increasing by <i>k</i>% per year.</p>	<p>Continuous Annuities</p> <p>PV of an <i>n</i>-year annuity paying continuously at a rate of <i>t</i>, with a constant FoI, δ.</p>																				
Section 04.k	Section 04.k	Section 04.l																				
<p>Continuous Annuities</p> <p>PV of an <i>n</i>-year annuity paying continuously at a rate of $f(t)$, with a constant FoI, δ.</p>	<p>Continuous Annuities</p> <p>Find PV of an <i>n</i>-year annuity paying continuously at a rate of $f(t)$, with a variable FoI, δ_t.</p>	<p>Palindromic Annuity</p> <p>PV of an annuity imm. paying: 1, 2, 3, ..., <i>n</i> - 1, <i>n</i>, <i>n</i> - 1, ..., 3, 2, 1</p>																				
Section 05.a	Section 05.a	Section 05.e																				
<p>Net Present Value</p> <p>Define NPV.</p>	<p>Internal Rate of Return</p> <p>Define IRR.</p>	<p>Find DWR for this example:</p> <table border="1"> <thead> <tr> <th></th> <th><i>t</i>=0</th> <th><i>t</i>=1/4</th> <th><i>t</i>=1/2</th> <th><i>t</i>=1</th> </tr> </thead> <tbody> <tr> <td>Beg:</td> <td>0</td> <td>120</td> <td>90</td> <td>220</td> </tr> <tr> <td>Trans</td> <td>+ 100</td> <td>- 40</td> <td>+ 110</td> <td>- 220</td> </tr> <tr> <td>End:</td> <td>100</td> <td>80</td> <td>200</td> <td>0</td> </tr> </tbody> </table>		<i>t</i> =0	<i>t</i> =1/4	<i>t</i> =1/2	<i>t</i> =1	Beg:	0	120	90	220	Trans	+ 100	- 40	+ 110	- 220	End:	100	80	200	0
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End:	100	80	200	0																		

$(Da)_{\overline{n} } = \frac{n - a_{\overline{n} }}{i}$ $(Ds)_{\overline{n} } = \frac{n(1+i)^n - s_{\overline{n} }}{i}$	$(Ia)_{\overline{n} } = \frac{\ddot{a}_{\overline{n} } - nv^n}{i}$ $(Is)_{\overline{n} } = \frac{\ddot{s}_{\overline{n} } - n}{i}$	$A = P a_{\overline{n} } + Q \frac{a_{\overline{n} } - nv^n}{i}$ $S = P s_{\overline{n} } + Q \frac{s_{\overline{n} } - n}{i}$
<p>PV of m-thly payments starting at $1/m$, and increasing by $1/m$ each year.</p> $(Ia)_{\overline{n} }^{(m)} = \frac{\ddot{a}_{\overline{n} } - nv^n}{i^{(m)}}$	$PV = \frac{\ddot{a}_{\overline{n} }}{i}$	$(Ia)_{\infty } = \frac{1}{id} = \frac{1}{i} + \frac{1}{i^2}$
$(\overline{Ia})_{\overline{n} } = \int_0^n tv^t dt = \frac{\overline{a}_{\overline{n} } - nv^n}{\delta}$	$PV = \frac{P}{1+k} a_{\overline{n} i'}$ <p>where $i' = \frac{i-k}{1+k}$</p>	<p>PV of m-thly payments starting at $1/m^2$, and increasing by $1/m^2$ each m-thly period.</p> $(I^{(m)}a)_{\overline{n} }^{(m)} = \frac{\ddot{a}_{\overline{n} }^{(m)} - nv^n}{i^{(m)}}$
$PV = a_{\overline{n} i} \cdot \ddot{a}_{\overline{n} i}$	$\int_0^n \frac{f(t)}{a(t)} dt$	$\int_0^n f(t)v^t dt$
$\text{DWR} = \frac{-100 + 40 - 110 + 220}{100(1) - 40(3/4) + 110(1/2)}$ $= 0.4 = 40\%$	<p>The rate at which the PV of cash inflows is equal to PV of cash outflows.</p>	<p>Sum the PV of cash inflows and cash outflows, calculated using the “interest preference rate”.</p>

Section 05.e	Section 06.a	Section 06.a																				
<p>Find DWR for this example:</p> <table border="1"> <thead> <tr> <th></th> <th>$t=0$</th> <th>$t=1/4$</th> <th>$t=1/2$</th> <th>$t=1$</th> </tr> </thead> <tbody> <tr> <td>Beg:</td> <td>0</td> <td>120</td> <td>90</td> <td>220</td> </tr> <tr> <td>Trans</td> <td>+ 100</td> <td>- 40</td> <td>+ 110</td> <td>- 220</td> </tr> <tr> <td>End:</td> <td>100</td> <td>80</td> <td>200</td> <td>0</td> </tr> </tbody> </table>		$t=0$	$t=1/4$	$t=1/2$	$t=1$	Beg:	0	120	90	220	Trans	+ 100	- 40	+ 110	- 220	End:	100	80	200	0	<p>Amortization</p> <p>1) Find B_t prospectively. 2) Find B_t retrospectively.</p>	<p>Amortization</p> <p>1) Give formulas for I_t. 2) Give formulas for P_t.</p>
	$t=0$	$t=1/4$	$t=1/2$	$t=1$																		
Beg:	0	120	90	220																		
Trans	+ 100	- 40	+ 110	- 220																		
End:	100	80	200	0																		
Section 06.b	Section 06.b	Section 06.b																				
<p>Sinking Funds</p> <p>1) Give formula for SFD. 2) Give formula for total payment under SF method.</p>																						
Section 07.b	Section 07.b	Section 07.b																				
<p>Bond Pricing</p> <p>State the relationship between the coupon rate and the special coupon rate.</p>	<p>Bond Pricing</p> <p>Give the basic bond pricing formula.</p>	<p>Bond Pricing</p> <p>State the premium/discount bond pricing formula.</p>																				
Section 07.c	Section 07.c	Section 07.c																				
<p>Premium and Discount</p> <p>Explain the relationships between P and C and g and i for a bond purchased at a premium.</p>	<p>Premium and Discount</p> <p>Explain the relationships between P and C and g and i for a bond purchased at a discount.</p>	<p>Premium and Discount</p> <p>For bonds sold at a premium, does the book value increase or decrease over time?</p>																				
Section 07.c	Section 07.c	Section 07.c																				
<p>Premium and Discount</p> <p>For bonds sold at a discount, does the book value increase or decrease over time?</p>	<p>Premium and Discount</p> <p>Give formula for Write-Down of Premium</p>	<p>Premium and Discount</p> <p>Give formula for Write-Up of Discount</p>																				

$I_t = R[1 - v^{n-t+1}] = iB_{t-1}$ $P_t = Rv^{n-t+1} = R - I_t$	$B_t = Ra_{\overline{n-t} }$ $B_t = L(1+i)^t - Rs_{\overline{t} }$	$\text{TWR} = \frac{120}{100} \frac{90}{80} \frac{220}{200} - 1$ $= 0.485 = 48.5\%$
		$\text{SFD} = \frac{L}{s_{\overline{n} j}}$ $R_t = Li + \frac{L}{s_{\overline{n} j}}$ <p>(i is rate on loan, j is SF rate)</p>
$P = C + (Fr - Ci)a_{\overline{n} i}$	$P = Fra_{\overline{n} i} + Cv^n$	$Cg = Fr$
<p>Premium:</p> <p>Book value decreases over time.</p> <p>This process is called “Write-Down” of premium.</p>	<p>Discount:</p> $P < C$ $g < i$	<p>Premium:</p> $P > C$ $g > i$
$P_t = (Ci - Fr)v^{n-t+1}$	$P_t = (Fr - Ci)v^{n-t+1}$	<p>Discount:</p> <p>Book value increases over time.</p> <p>This process is called “Write-Up” of discount.</p>

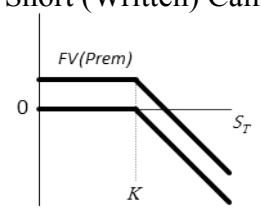
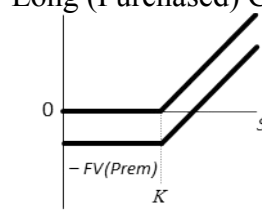
Section 07.d	Section 07.d	Section 07.f
<p>Price Between Coupons</p> <p>Give the Full Price (also called the Dirty Price).</p>	<p>Price Between Coupons</p> <p>Give the Market Price (also called the Clean Price).</p>	<p>Callable Bonds</p> <p>For a bond selling at a premium, is an earlier redemption date better or worse?</p>
Section 07.f	Section 08.b	Section 08.b
<p>Callable Bonds</p> <p>For a bond selling at a discount, is an earlier redemption date better or worse?</p>	<p>Preferred Stock</p> <p>Give the price of a preferred stock paying coupons of $F r$.</p>	<p>Common Stock</p> <p>Give the theoretical price of a common stock with expected dividend of D and growth rate k.</p>
Section 09.a	Section 09.b	Section 09.b
<p>Inflation</p> <p>Given an effective rate of i, and an inflation rate of r, find the real rate of interest, i'.</p>	<p>Spot Rates and Forward Rates</p> <p>Given spot rates s_1, s_2, \dots, find a formula for the forward rate f_n.</p>	<p>Spot Rates and Forward Rates</p> <p>Given forward rates f_1, f_2, \dots, find a formula for the spot rate s_n.</p>
Section 09.d	Section 09.d	Section 09.e
<p>Duration and Convexity</p> <p>Give the formula for Macaulay Duration.</p>	<p>Duration and Convexity</p> <p>Give the Macaulay Duration for a zero coupon bond.</p>	<p>Duration and Convexity</p> <p>Give the derivative definition for Macaulay Duration.</p>
Section 09.f	Section 09.f	Section 09.g
<p>Duration and Convexity</p> <p>Give the derivative definition for Modified Duration.</p>	<p>Duration and Convexity</p> <p>State the relationship between $ModD$ and $MacD$.</p>	<p>Duration and Convexity</p> <p>Assume a portfolio contains n investments, each with present value PV_i and duration $ModD_i$. Find the duration of the portfolio.</p>

<p>For a bond selling at a premium, an earlier redemption date is worse.</p>	$B_{t+k} - kFr = B_t(1+i)^k - kFr$	$B_{t+k} = B_t(1+i)^k$
$P = \frac{D}{i-k}$	$P = \frac{Fr}{i}$	<p>For a bond selling at a discount, an earlier redemption date is better.</p>
$(1+s_n)^n = (1+f_0) \cdot (1+f_1) \cdot \dots \cdot (1+f_{n-1})$	$1+f_n = \frac{(1+s_{n+1})^{n+1}}{(1+s_n)^n}$	$i' = \frac{i-r}{1+r}$
$MacD = -\frac{P'(\delta)}{P(\delta)}$	<p>$MacD = n$ for a zero coupon bond</p>	$MacD = \frac{\sum (t \cdot v^t \cdot CF_t)}{\sum (v^t \cdot CF_t)}$
$ModD = \frac{\sum (PV_i \cdot ModD_i)}{\sum PV_i}$	$ModD = v \cdot MacD$	$ModD = -\frac{P'(i)}{P(i)}$

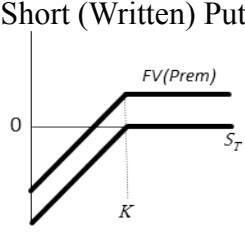
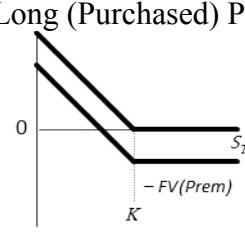
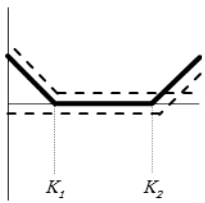
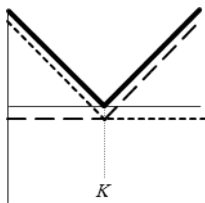
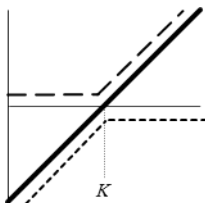
Section 09.i	Section 09.i	Section 09.i
<p>Duration and Convexity</p> <p>Give the derivative definition for Convexity.</p>	<p>Duration and Convexity</p> <p>Give the formula for Convexity.</p>	<p>Duration and Convexity</p> <p>Give the Taylor Polynomial approximation for ΔP, given Δi.</p>
Section 09.j	Section 09.k	Section 09.j
<p>Immunization</p> <p>State the criteria for Redington Immunization. What is the effect of Redington Immunization?</p>	<p>Immunization</p> <p>State the criteria for Full Immunization. What is the effect of Full Immunization?</p>	<p>Immunization</p> <p>State the criteria for Duration Matching.</p>
Section 10	Section 10	Section 10
<p>Buying and Selling Assets</p> <p>As an individual buying an asset, do you pay the ask price, or the bid price?</p>	<p>Buying and Selling Assets</p> <p>As an individual selling an asset, do you receive the ask price, or the bid price?</p>	<p>Buying and Selling Assets</p> <p>Which is larger: The ask price, or the bid price?</p>
Section 10	Section 10	Section 10
<p>Buying and Selling Assets</p> <p>Does a broker buying an asset pay the ask price or the bid price?</p>	<p>Buying and Selling Assets</p> <p>Does a broker selling an asset receive the ask price or the bid price?</p>	<p>Derivatives</p> <p>State four reasons for using derivatives.</p>
Section 10	Section 10	Section 10
<p>Long vs Short Positions</p> <p>If you have a long position in an asset, do you benefit from an increase or decrease in the price of that asset?</p>	<p>Long vs Short Positions</p> <p>If you have a short position in an asset, do you benefit from an increase or decrease in the price of that asset?</p>	<p>Short-Selling</p> <p>Describe the basic process of a short-sale, ignoring haircuts and dividends.</p>

$\Delta P \approx P(i) \cdot \left[-(\Delta i) ModD + \frac{1}{2} (\Delta i)^2 (Conv) \right]$	$Conv = \frac{\sum [t(t+1)v^{t+2} CF_t]}{\sum (v^t \cdot CF_t)}$	$Conv = -\frac{P''(i)}{P(i)}$
$PV_A = PV_L$ $ModD_A = ModD_L$	$PV_A = PV_L$ $ModD_A = ModD_L$ <p>Each liability falls between two assets.</p> <p>Full Immunization protects against all changes in i.</p>	$PV_A = PV_L$ $ModD_A = ModD_L$ $Conv_A > Conv_L$ <p>Redington Immunization protects against small changes in i.</p>
<p>The ask price is larger than the bid price.</p>	<p>Individuals sell at the bid price.</p>	<p>Individuals buy at the ask price.</p>
<ol style="list-style-type: none"> 1. Risk management - hedging 2. Speculation - investment vehicle 3. Reducing transaction costs 4. Regulatory arbitrage 	<p>Brokers sell at the ask price.</p>	<p>Brokers buy at the bid price.</p>
<p>Short Selling:</p> <ol style="list-style-type: none"> 1. Borrow a share of the stock, and sell it immediately. 2. Close the short at a later date by purchasing a share of the stock and returning it to the original lender. 	<p>Short positions benefit from a decrease in the price of the underlying asset.</p>	<p>Long positions benefit from an increase in the price of the underlying asset.</p>

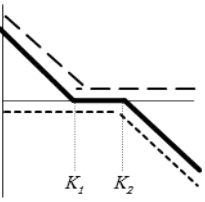
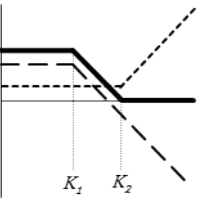
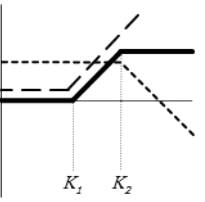
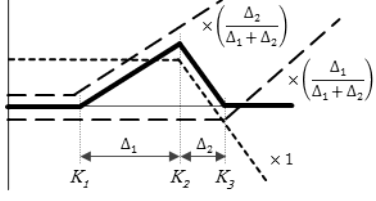
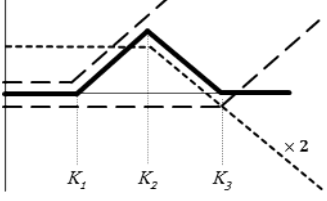
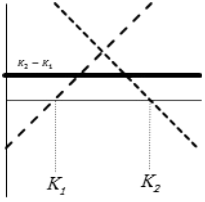

Section 10	Section 10	Section 10
<p>Short-Selling</p> <p>What is a haircut (also called margin)?</p>	<p>Short-Selling</p> <p>What is the maximum loss that can be incurred as a result of a short-sell?</p>	<p>Short-Selling</p> <p>List three reasons for short-selling.</p>
Section 11	Section 11	Section 11
<p>Forward Contracts</p> <p>State the payoff of a long forward contract.</p>	<p>Forward Contracts</p> <p>State the payoff of a short forward contract.</p>	<p>Forward Contracts</p> <p>What is the relationship between payoff and profit for a forward contract?</p>
Section 12	Section 12	Section 12
<p>Call Options</p> <p>Describe a call option.</p>	<p>Call Options</p> <p>Give formulas for payoff and profit for a long call and a short call.</p>	<p>Call Options</p> <p>What positions do the sides of a call option hold with respect to the underlying asset?</p>
Section 12	Section 12	
<p>Call Options</p> <p>Sketch graphs of payoff and profit for a long call.</p>	<p>Call Options</p> <p>Sketch graphs of payoff and profit for a short call.</p>	
Section 13	Section 13	Section 13
<p>Put Options</p> <p>Describe a put option.</p>	<p>Put Options</p> <p>Give formulas for payoff and profit for a long put and a short put.</p>	<p>Put Options</p> <p>What positions do the sides of a put option hold with respect to the underlying asset?</p>

<ol style="list-style-type: none"> To speculate that the price of the asset will decline. To borrow money for financing purposes. To hedge the risk of owning an asset or a derivative on the asset. 	<p>The potential loss on a short-sale is unlimited.</p>	<p>A haircut (or margin) is collateral given to the lender by the short-seller.</p>
<p>Since the only transactions take place at time T, payoff and profit are the same for a forward contract.</p>	<p>Payoff for short forward =</p> $F - S_T$	<p>Payoff for long forward =</p> $S_T - F$
<p>A long (or purchased) call is long with respect to the underlying asset.</p> <p>A short (or written) call is short with respect to the underlying asset.</p>	<p>Long Call</p> <ul style="list-style-type: none"> $PO = \max[0, S_T - K]$ Profit = PO – FV(Prem) <p>Long Call</p> <ul style="list-style-type: none"> $PO = -\max[0, S_T - K]$ Profit = PO + FV(Prem) 	<p>The purchaser of a call option has the right (but not the obligation) to buy for K on the exercise date.</p> <p>The writer of a call option has an obligation to sell for K if the call is exercised.</p>
	<p>Short (Written) Call</p> 	<p>Long (Purchased) Call</p> 
<p>A long (or purchased) put is short with respect to the underlying asset.</p> <p>A short (or written) put is long with respect to the underlying asset.</p>	<p>Long Put</p> <ul style="list-style-type: none"> $PO = \max[0, K - S_T]$ Profit = PO – FV(Prem) <p>Long Put</p> <ul style="list-style-type: none"> $PO = -\max[0, K - S_T]$ Profit = PO + FV(Prem) 	<p>The purchaser of a put option has the right (but not the obligation) to sell for K on the exercise date.</p> <p>The writer of a put option has an obligation to buy for K if the put is exercised.</p>

Section 13	Section 13	
<p>Put Options</p> <p>Sketch graphs of payoff and profit for a long put.</p>	<p>Put Options</p> <p>Sketch graphs of payoff and profit for a short put.</p>	
Sections 12 and 13	Section 14	Section 15
<p>Option Styles</p> <p>Describe the difference between American-style options and European-style options.</p>	<p>Option Moneyness</p> <p>Describe the following terms:</p> <ol style="list-style-type: none"> 1. In-the-money 2. At-the-money 3. Out-of-the-money 	<p>Hedging Strategies</p> <ol style="list-style-type: none"> 1. Describe the assets used to create a protective put. 2. In terms of profit, a protective put is the same as what option?
Section 15	Section 15	Section 15
<p>Hedging Strategies</p> <ol style="list-style-type: none"> 1. Describe the assets used to create a covered call. 2. In terms of profit, a covered call is the same as what option? 	<p>Hedging Strategies</p> <ol style="list-style-type: none"> 1. Describe the assets used to create a covered put. 2. In terms of profit, a covered put is the same as what option? 	<p>Hedging Strategies</p> <ol style="list-style-type: none"> 1. Describe the assets used to create a protective call. 2. In terms of profit, a protective call is the same as what option?
Section 16	Section 16	Section 16
<p>Put-Call Parity</p> <p>State the general formula for Put-Call Parity</p>	<p>Put-Call Parity</p> <p>State the Put-Call Parity formula for a non-dividend paying stock.</p>	<p>Arbitrage</p> <p>Define arbitrage.</p>
Section 16	Section 16	Section 16
<p>Combining Options</p> <ol style="list-style-type: none"> 1. Sketch the graph of the payoff of a synthetic forward. 2. Describe the options used to construct a synthetic forward. 	<p>Combining Options</p> <ol style="list-style-type: none"> 1. Sketch the graph of the payoff of a straddle. 2. Describe the options used to construct a straddle. 	<p>Combining Options</p> <ol style="list-style-type: none"> 1. Sketch the graph of the payoff of a $K_1 - K_2$ strangle. 2. Describe the options used to construct a $K_1 - K_2$ strangle.

	<p style="text-align: center;">Short (Written) Put</p> 	<p style="text-align: center;">Long (Purchased) Put</p> 
<ol style="list-style-type: none"> Protective Put = Long Asset + Long Put In terms of profit: Long Asset + Long Put = Long Call 	<ol style="list-style-type: none"> In-the-money: Positive payoff if the option is exercised now. At-the-money: Spot price is currently equal to strike price. Out-of-the-money: Negative PO if the option is exercised now. 	<p>European-style options may only be exercised on the exercise date.</p> <p>American-style options may be exercised at any time prior to the exercise date.</p>
<ol style="list-style-type: none"> Covered Call = Long Asset + Short Call In terms of profit: Long Asset + Short Call = Short Put 	<ol style="list-style-type: none"> Covered Put = Short Asset + Short Put In terms of profit: Short Asset + Short Put = Short Call 	<ol style="list-style-type: none"> Protective Call = Short Asset + Long Call In terms of profit: Short Asset + Long Call = Long Put
<p>A transaction which generates a positive cash flow with no net investment or risk.</p>	$Call - Put = S_0 - PV(K)$	$Call - Put = PV(F_{0,T}) - PV(K)$ $Call - Put = F_{0,T}^P - PV(K)$
 <p>K_1 - Strike Long Put K_2 - Strike Long Call</p>	 <p>K - Strike Long Call K - Strike Long Put</p>	 <p>K - Strike Long Call K - Strike Short Put</p>

Section 16	Section 16	Section 16
<p>Combining Options</p> <ol style="list-style-type: none"> 1. Sketch the graph of the payoff of a K_1-K_2 collar. 2. Describe the options used to construct a K_1-K_2 collar. 	<p>Combining Options</p> <ol style="list-style-type: none"> 1. Sketch the graph of the payoff of a K_1-K_2 bear spread. 2. Describe the options used to build a K_1-K_2 bear spread. 	<p>Combining Options</p> <ol style="list-style-type: none"> 1. Sketch the graph of the payoff of a K_1-K_2 bull spread. 2. Describe the options used to build a K_1-K_2 bull spread.
Section 16	Section 16	Section 16
<p>Combining Options</p> <ol style="list-style-type: none"> 1. Sketch the graph of the PO of a $K_1-K_2-K_3$ asymm butterfly. 2. Describe the options used in a $K_1-K_2-K_3$ asymm butterfly. 	<p>Combining Options</p> <ol style="list-style-type: none"> 1. Sketch the graph of the PO of a $K_1-K_2-K_3$ symm butterfly. 2. Describe the options used in a $K_1-K_2-K_3$ symm butterfly. 	<p>Combining Options</p> <ol style="list-style-type: none"> 1. Sketch the graph of the payoff of a K_1-K_2 box spread. 2. Describe the options used to build a K_1-K_2 box spread.
Section 17	Section 17	Section 16
<p>Hedging</p> <p>List six potential reasons to hedge.</p>	<p>Hedging</p> <p>List four potential reasons not to hedge.</p>	<p>Combining Options</p> <ol style="list-style-type: none"> 1. Sketch the graph of the payoff of a ratio spread. 2. Describe the options used to construct a ratio spread.
Section 18	Section 18	Section 18
<p>Cash-and-Carry</p> <ol style="list-style-type: none"> 1. Describe a cash-and-carry strategy. 2. What is the purpose of a cash-and-carry strategy? 	<p>Reverse Cash-and-Carry</p> <ol style="list-style-type: none"> 1. Describe a reverse cash-and-carry strategy. 2. What is the purpose of a reverse cash-and-carry strategy? 	<p>Futures Contracts</p> <p>List four ways in which a futures contract differs from a forward contract.</p>
Section 19	Section 19	Section 19
<p>Commodity Swaps</p> <p>Describe a commodity swap.</p>	<p>Commodity Swaps</p> <p>Describe a market value of a commodity swap.</p>	<p>Interest Rate Swaps</p> <p>Consider a three year period with spot rates s_1, s_2, and s_3. Provide a formula that could be used to find the fixed swap rate R.</p>

 <p> K_1 - Strike Long Put K_2 - Strike Short Call </p>	 <p> K_1 - Strike Short Call K_2 - Strike Long Call or K_1 - Strike Short Put K_2 - Strike Long Put (PO shifted down) </p>	 <p> K_1 - Strike Long Call K_2 - Strike Short Call or K_1 - Strike Long Put K_2 - Strike Short Put (PO shifted down) </p>
 <p> K_1 - Strike Long Call ($\times \lambda_1$) $\lambda_1 = \frac{\Delta_2}{\Delta_1 + \Delta_2}$ K_2 - Strike Short Call ($\times 1$) K_3 - Strike Long Call ($\times \lambda_2$) $\lambda_2 = \frac{\Delta_1}{\Delta_1 + \Delta_2}$ </p>	 <p> K_1 - Strike Long Call K_2 - Straddle (Short) K_2 - Strike Short Call ($\times 2$) $K_1 - K_3$ - Strangle (Long) K_3 - Strike Long Call </p>	 <p> K_1 - Long Syn Fwd K_2 - Short Syn Fwd </p>
<p>Reasons not to hedge:</p> <ol style="list-style-type: none"> 1. Involves transaction costs 2. Potentially costly expertise 3. Monitoring and control capabilities 4. Financial reporting, accounting, and tax considerations 	<p>Reasons to hedge:</p> <ol style="list-style-type: none"> 1. Decrease taxes 2. Reduce chance of bankruptcy 3. Financing – Alternative to borrowing 4. Increase debt capacity 5. Risk aversion 6. Manage non-financial risks 	 <p> K - Strike Long Call K - Strike Short Put </p>
<p>Futures Contracts</p> <ol style="list-style-type: none"> 1. Traded on an exchange 2. Relatively standardized 3. More liquid than forwards 4. Marked-to-market and settled daily 	<p>Reverse Cash-and-Carry</p> <ol style="list-style-type: none"> 1. Long forward + Short asset 2. Arbitrage strategy to take advantage of a forward price that is too low. 	<p>Cash-and-Carry</p> <ol style="list-style-type: none"> 1. Short forward + Long asset 2. Arbitrage strategy to take advantage of a forward price that is too high.
$1 = \frac{R}{1+s_1} + \frac{R}{(1+s_2)^2} + \frac{1+R}{(1+s_3)^3}$	<p>Market value of swap contract is 0 when contract is entered into. Lending/borrowing will occur with the first payment. After that point, the swap will generally have a nonzero market value.</p>	<p>A commodity swap involves the exchange of a variable sequence of payments with a sequence of level payments.</p>

Section 18	Section 18	Section 18
<p>Forward Prices</p> <p>Give the forward price of a stock that pays no dividends.</p>	<p>Forward Prices</p> <p>Give the forward price of a stock paying discrete dividends.</p>	<p>Forward Prices</p> <p>Give the forward price of a stock paying continuous dividends.</p>
Section 18	Section 18	Section 18
<p>Prepaid Forward Prices</p> <p>Give the prepaid forward price of a stock that pays no dividends.</p>	<p>Prepaid Forward Prices</p> <p>Give the prepaid forward price of a stock paying discrete dividends.</p>	<p>Prepaid Forward Prices</p> <p>Give the prepaid forward price of a stock paying continuous dividends.</p>
Section 18		
<p>Forward Prices</p> <p>State the relationship between the forward and prepaid forward prices of an asset.</p>		

$F_{0,T} = S_0 e^{(r-\delta)T}$	$F_{0,T} = S_0 e^{rT} - AV(\text{Divs})$	$F_{0,T} = S_0 e^{rT}$
$F_{0,T}^P = S_0 e^{-\delta T}$	$F_{0,T}^P = S_0 - PV(\text{Divs})$	$F_{0,T}^P = S_0$
		$F_{0,T}^P = PV(F_{0,T}) = F_{0,T} e^{-rT}$ $F_{0,T} = AV(F_{0,T}^P) = F_{0,T}^P e^{rT}$